

Math 301

Quiz 4

Justify all answers with neat and organized work. Clearly indicate your answers. 20 points possible.

1. (5 pts.) Let A be the set of all integers from 1 through 1,000 that are multiples of 4 or multiples of 11. How many elements are in A ?

2. (5 pts.) Determine how many times the innermost loop will be iterated when the algorithm segment is implemented and run.

```
for  $i := 15$  to 80
  for  $j := 30$  to 60
    [Statements in body of inner loop. None contain branching statements
     that lead outside the loop.]
  next  $j$ 
next  $i$ 
```

3. (5 pts.) Suppose $A[1], A[2], \dots, A[2n]$, is a one-dimensional array and $n \geq 2$. What is the probability that a randomly chosen array element is in the subarray

$$A[1], A[2], \dots, A[\lfloor 3n/2 \rfloor]$$

(a) if n is even?

(b) if n is odd?

4. (5 pts.) Let $B = \{n \in \mathbb{Z} \mid 1 \leq n \leq 400\}$.

(a) How many even integers are in B ?

(b) How many odd integers are in B ?

(c) How many ways can two different integers be selected from B so that their sum is even?

(d) How many ways can two different integers be selected from B so that their sum is odd?